We first handle the case where the f.c. group G is finitely generated, say by $\{g_1, \ldots, g_m\}$. Here, $Z(G) = \bigcap_{i=1}^{m} C_G(g_i)$ is of finite index, so $/[G,G]/ < \infty$.