

Clearly,  $\text{rad } R$  is the ideal generated by the  $x_i$ 's. We have  $(\text{rad } R)^2 = 0$ , and  $R/\text{rad } R \sim \mathbb{Q}$ , so  $R$  is semiprimary. The strictly ascending chain  $(x_1) \subseteq (x_1, x_2) \subseteq (x_1, x_2, x_3) \subseteq \dots$  shows that  $R$  is not noetherian, while the strictly descending chain  $(x_1, x_2, \dots) \supseteq (x_2, x_3, \dots) \supseteq (x_3, x_4, \dots) \supseteq \dots$  shows that  $R$  is not artinian.