

We can transform this equation using the next trigonometric identities:

$$\sec x = \frac{1}{\cos x} \text{ and } \cos(90^\circ - x) = \sin x$$

We have:

$$\frac{1}{\cos(2x)} = 3\cos(2x) + \sin(2x)$$

Since $\sin x = \sqrt{1 - \cos^2 x}$ then:

$$\frac{1}{\cos(2x)} = 3\cos(2x) + \sqrt{1 - \cos^2(2x)}$$

After the substitution $\cos(2x) = t$ we get the equation:

$$\frac{1}{t} = 3t + \sqrt{1 - t^2}$$

The roots of this equation are: $-\frac{\sqrt{2}}{2}$ and $\frac{\sqrt{5}}{5}$

We have two equations for $\cos(2x)$:

$$\cos(2x) = -\frac{\sqrt{2}}{2}$$

$$\cos(2x) = \frac{\sqrt{5}}{5}$$

First equation gives $x = \pm \frac{1}{2} \arccos\left(-\frac{\sqrt{2}}{2}\right) = \pm 67.5^\circ$

From second equation $x = \pm \frac{1}{2} \arccos\left(-\frac{\sqrt{5}}{5}\right) \approx \pm 31.7^\circ$

Answer : $x = \{-67.5^\circ, -31.7^\circ, 31.7^\circ, 67.5^\circ\}$