9a. $\sqrt{5 y+1}+4=0 \quad, \quad \sqrt{5 y+1}=-4$. Range of square root on the left: $\quad y \geq-\frac{1}{5}$.
Exponentiating both sides of equation, obtain $5 y+1=16, y=\frac{15}{5}=3$. This solution satisfies the domain, so this is the solution of equation.

9b. $\quad 1+\sqrt{x+1}=\sqrt{2 x+3}$. First, find domains of squares: $\quad x \geq-1, x \geq \frac{-3}{2} \Rightarrow x \geq-1$.
Exponentiating both sides of equation, obtain
$1+x+1+2 \sqrt{x+1}=2 x+3,2 \sqrt{x+1}=x+1,4(x+1)=x^{2}+2 x+1 \Rightarrow x_{1,2}=-1 ; 3$. Both solutions satisfy domains of squares, hence the solution of equation is $x=-1 ; x=3$.

