Question 22488

9a. $\sqrt{5y+1}+4=0$, $\sqrt{5y+1}=-4$. Range of square root on the left: $y \ge -\frac{1}{5}$.

Exponentiating both sides of equation, obtain 5y+1=16, $y=\frac{15}{5}=3$. This solution satisfies the domain, so this is the solution of equation.

9b. $1 + \sqrt{x+1} = \sqrt{2x+3}$. First, find domains of squares: $x \ge -1, x \ge \frac{-3}{2} \Rightarrow x \ge -1$.

Exponentiating both sides of equation, obtain

 $1+x+1+2\sqrt{x+1}=2x+3$, $2\sqrt{x+1}=x+1$, $4(x+1)=x^2+2x+1\Rightarrow x_{1,2}=-1$; 3. Both solutions satisfy domains of squares, hence the solution of equation is x=-1; x=3.