

$$\tan A + \cot A = 2 \operatorname{cosec} 2A$$

Using the definitions of the trigonometric functions

$$\tan A = \frac{\sin A}{\cos A} \text{ and } \cot A = \frac{\cos A}{\sin A}, \text{ so}$$

$$LH = \tan A + \cot A = \frac{\sin A}{\cos A} + \frac{\cos A}{\sin A} = \frac{\sin^2 x + \cos^2 x}{\cos A \sin A}$$

Using the Pythagorean identities

$$\sin^2 x + \cos^2 x = 1$$

Using the double-angle formulae

$$\cos A \sin A = \frac{1}{2} \sin 2A$$

$$LH = \frac{\sin^2 x + \cos^2 x}{\cos A \sin A} = \frac{1}{\frac{1}{2} \sin 2A} = \frac{2}{\sin 2A}$$

Using the definitions of the trigonometric functions

$$\operatorname{cosec} 2A = \frac{1}{\sin 2A}, \text{ so}$$

$$RH = \frac{2}{\sin 2A}, \text{ so } LH = RH$$