

## Conditions

One of the following is false

(A)  $A \cup B = \{x : x \in A \text{ or } x \in B\}$

(B)  $A \setminus (B \cup C) = (A \setminus B) \cap (A \setminus C)$

(C)  $A \setminus (B \cup C) = (A \setminus B) \cup (A \setminus C)$

(D)  $A \setminus (B \cap C) = (A \setminus B) \cup (A \setminus C)$

Please explain

## Solution

The false statement is C.

Explanation:

Consider point  $b$  from set  $A$  and  $B$  but not from  $C$ :

$$b \in A \cap B, b \notin C = \emptyset$$

Consider set  $A \setminus (B \cup C)$ .  $b$  is not from this set, as  $b \in A \cap B, \rightarrow, b \in B$ :

$$b \notin A \setminus (B \cup C) = \emptyset$$

Consider set  $(A \setminus B) \cup (A \setminus C)$ . The first set doesn't have point  $b$  in it, as  $b$  is from  $B$ , but the second set has this point in, because  $b$  is from  $A$ , but  $b$  isn't from  $C$ , so if we exclude all  $C$  points from  $A$ , there will remain our point  $b$ . As we have a  $\cup$  between, it means, that there is point  $b$  in  $(A \setminus B) \cup (A \setminus C)$

So, on the left side of this set equation we have a set, which doesn't include point  $b$  and on the right side – a set which includes this point. **Here is a false.**