

Show that

$$\frac{\sqrt{1 - \cot^2 x} * \sqrt{\tan^2 x}}{\cos x} = \tan 2x$$

Solution:

$$\begin{aligned} \frac{\sqrt{1 - \cot^2 x} * \sqrt{\tan^2 x}}{\cos x} &= \frac{\sqrt{\left(1 - \left(\frac{\cos x}{\sin x}\right)^2\right) * \frac{\sin^2 x}{\cos^2 x}}}{\cos x} = \frac{\sqrt{\left(\frac{\sin^2 x - \cos^2 x}{\sin^2 x}\right) * \frac{\sin^2 x}{\cos^2 x}}}{\cos x} \\ &= \frac{\sqrt{\sin^2 x - \cos^2 x}}{\cos^2 x} \neq \tan 2x \end{aligned}$$

For example take 60°

$$\tan 60^\circ = \sqrt{3}$$

$$\cot 60^\circ = \frac{1}{\sqrt{3}}$$

$$\tan 120^\circ = -\sqrt{3}$$

$$\cos 60^\circ = \frac{1}{2}$$

$$\frac{\sqrt{1 - \cot^2 x} * \sqrt{\tan^2 x}}{\cos x} = \frac{\sqrt{1 - \frac{1}{3}\sqrt{3}}}{2} = \frac{\sqrt{2}}{2}$$

$$\tan 2x = \tan 120^\circ = -\sqrt{3}$$

$$\frac{\sqrt{2}}{2} \neq -\sqrt{3}$$