

derivative of $x^{\ln x}$

Solution:

$$\begin{aligned}(x^{\ln x})' &= (e^{\ln(x^{\ln x})})' = e^{\ln(x^{\ln x})} * \ln e * (\ln(x^{\ln x}))' = x^{\ln x} * (\ln x * \ln x)' = x^{\ln x} * ((\ln x)^2)' \\ &= x^{\ln x} * 2 \ln x * (\ln x)' = x^{\ln x} * 2 \ln x * \frac{1}{x} = x^{\ln x - 1} * 2 \ln x\end{aligned}$$

Answer: $x^{\ln x - 1} * 2 \ln x$