

Task:

If $f = (1, 2), (2, 3), (3, 4), (4, 5)$, $g = (1, -2), (3, -3), (5, -5)$, $h = (1, 0), (2, 1), (3, 2)$,

find the following and state the domain

2a. $f + g$

2b. $f - g$

2c. $f \cdot g$

Solution:

If f and g are functions and (x,y) are some points of these functions, then we can conclude that

$$f(x) = x + 1$$

Using a simple method of multivariate interpolation (nearest-neighbor interpolation)

$$g(x) = -0.125x^2 - 3.1755711 \cdot 10^{-17}x - 1.875$$

Answer:

$$\begin{aligned} 2a. f(x) + g(x) &= x + 1 - 0.125x^2 - 3.1755711 \cdot 10^{-17}x - 1.875 = \\ &= -0.125x^2 - (3.1755711 \cdot 10^{-17} - 1)x + 0.875 \approx \\ &\approx -0.125x^2 + x + 0.875 \end{aligned}$$

$$\begin{aligned} 2b. f(x) - g(x) &= x + 1 + 0.125x^2 + 3.1755711 \cdot 10^{-17}x + 1.875 = \\ &= 0.125x^2 + (3.1755711 \cdot 10^{-17} + 1)x + 2.875 \approx \\ &\approx 0.125x^2 + x + 2.875 \end{aligned}$$

$$\begin{aligned} 2c. f(x) \cdot g(x) &= (-0.125x^2 - 3.1755711 \cdot 10^{-17}x - 1.875)(x + 1) = \\ &\approx -0.125x^3 - 0.125x^2 - 1.875x - 1.875 \end{aligned}$$