let $A B C D$ be an isosceles trapezoid with three of the vertices being $A(5,5), B(-1,3)$ and $C(3,-3)$. If line $A B$ forms one leg, then what is the length of line CD?
A
D

B

It's a strange task. I don't understand why we need coordinates of point C. It is unnecessary. It will have sense if $A B$ will be one of bases.

If line $A B$ forms one leg, then $C D$ forms another leg. $A B C D$ is an isosceles trapezoid than $A B=C D$.
Let we have 2 points $A\left(x_{1}, y_{1}\right)$ and $B\left(x_{2}, y_{2}\right)$, then $A B=\sqrt{\left(x_{2}-x_{1}\right)^{2}+\left(y_{2}-y_{1}\right)^{2}}$.
In our case: $A B=\sqrt{(-1-5)^{2}+(3-5)^{2}}=\sqrt{36+4}=\sqrt{40}=2 \sqrt{10}=C D$.
Answer: $2 \sqrt{10}$

