

Question#20645

solve the triangle : BC=1140in, AC=854in, AB=771in

Solution

Using the law of cosines find the angle A:

$$\begin{aligned}BC^2 &= AC^2 + AB^2 - 2 \cdot AC \cdot AB \cdot \cos(A); \\ \cos(A) &= \frac{AC^2 + AB^2 - BC}{2 \cdot AC \cdot AB}; \\ \cos(A) &= \frac{854^2 + 771^2 - 1140^2}{2 \cdot 854 \cdot 771} = 0,018344; \\ A &= 88,95^\circ;\end{aligned}$$

Next using the law of sines:

$$\begin{aligned}\frac{BC}{\sin(A)} &= \frac{AC}{\sin(B)}; \\ \sin(B) &= \frac{AC \cdot \sin(A)}{BC}; \\ \sin(B) &= \frac{854 \cdot 0,9998}{1140} = 0,748997; \\ B &= 48,5^\circ\end{aligned}$$

And finally the rule of angels of triangles gives us:

$$\begin{aligned}A + B + C &= 180^\circ; \\ C &= 180^\circ - A - B; \\ C &= 32,55^\circ;\end{aligned}$$

Answer:

$$A = 88,95^\circ; B = 48,5^\circ; C = 32,55^\circ;$$