

Conditions

$\sin 4A + \sin 2A / 1 + \cos 2A + \cos 4A = \tan 2A$ (prove this)

$\sin 3A - \sin A / \cos 3A + \cos A = \tan A$ (prove)

Solution

$$\frac{\sin 4a + \sin 2a}{1 + \cos 2a + \cos 4a} = \tan 2a$$

$$\begin{aligned} \frac{\sin 4a + \sin 2a}{1 + \cos 2a + \cos 4a} &= \frac{2 \sin 2a \cos 2a + \sin 2a}{\cos^2 2a + \sin^2 2a + \cos 2a + \cos^2 2a - \sin^2 2a} \\ &= \frac{\sin 2a (2 \cos 2a + 1)}{\cos 2a (2 \cos 2a + 1)} = \tan 2a \end{aligned}$$

$$\frac{\sin 3a - \sin a}{\cos 3a + \cos a} = \tan a$$

$$\frac{\sin 3a - \sin a}{\cos 3a + \cos a} = \frac{2 \sin a \cos 2a}{2 \cos 2a \cos a} = \frac{\sin a}{\cos a} = \tan a$$