

Conditions

A certain culture initially contains 10000 bacteria and increases 20% every hour.

- a) Find a formula for the number $N(t)$ of bacteria present after t hours.
- b) How many bacteria are in the culture at the end of 10 hours?

Solution

First off all we must say, that we are considering the case, when 20% is an addition to a total amount of bacteria in the end of previous hour. It means, that if after 1st hour there were $10000 + 10000 \cdot 20\% = 12000$ bacteria, then after 2nd hour there will be $12000 + 12000 \cdot 20\% = 14400$ bacteria, and so on and so forth.

a)

$$N(t) = 10000(1 + 0.2)^t, \text{ where } t \text{ is a passed time, in hours}$$

b)

$$N(10) = 10000(1.2)^{10} \approx 61917$$

61917 bacteria will be at the end of 10 hours.