

What is the derivative quotient of $\frac{6x-5}{2x-1}$?

Solution:

The rule states that the derivative of $\frac{f(x)}{g(x)}$ is

$$\left(\frac{f(x)}{g(x)}\right)' = \frac{f'(x)g(x) - g'(x)f(x)}{g^2(x)}$$

For $\frac{6x-5}{2x-1}$ it will be

$$\begin{aligned}\left(\frac{6x-5}{2x-1}\right)' &= \frac{(6x-5)'(2x-1) - (2x-1)'(6x-5)}{(2x-1)^2} = \frac{6(2x-1) - 2(6x-1)}{(2x-1)^2} \\ &= \frac{12x-6-12x+2}{(2x-1)^2} = \frac{-4}{(2x-1)^2}\end{aligned}$$

Answer: $\frac{-4}{(2x-1)^2}$