

How do I integrate this problem?? $\int (\sec 2x + \tan 2x) dx$

Solution:

$$\begin{aligned}\int (\sec 2x + \tan 2x) dx &= \int \sec 2x dx + \int \tan 2x dx = \int \frac{1}{\cos 2x} dx + \int \frac{\sin 2x}{\cos 2x} dx \\ &= \int \frac{\cos 2x}{\cos^2 2x} dx + \int \frac{\sin 2x dx}{\cos 2x} = \int \frac{\cos 2x dx}{1 - \sin^2 2x} \\ &+ \frac{1}{2} \int -\frac{d(\cos 2x)}{\cos 2x} = \frac{1}{2} \int \frac{d(\sin 2x)}{(1 - \sin 2x)(1 + \sin 2x)} - \frac{1}{2} \ln |\cos 2x| + C_1 \\ &= \frac{1}{2} \left(\int \frac{d(\sin 2x)}{1 - \sin 2x} + \int \frac{d(\sin 2x)}{1 + \sin 2x} \right) - \frac{1}{2} \ln |\cos 2x| + C_1 \\ &= \frac{1}{2} \left(\int \frac{-d(1 - \sin 2x)}{1 - \sin 2x} + \int \frac{d(1 + \sin 2x)}{1 + \sin 2x} \right) - \frac{1}{2} \ln |\cos 2x| + C_1 \\ &= \frac{1}{2} (\ln |1 + \sin 2x| - \ln |1 - \sin 2x| - \ln |\cos 2x|) + C \\ &= \frac{1}{2} \ln \left| \frac{1 + \sin 2x}{(1 - \sin 2x) * \cos 2x} \right| + C\end{aligned}$$