

Question

Graph of the function $f(x) = \frac{x+1}{x^2-1}$:

$$f(x) = \frac{x+1}{x^2-1} = \frac{1}{x-1}$$

$$f'(x) = -\frac{1}{(x-1)^2}$$

$$f''(x) = \frac{2}{(x-1)^3}$$

- domain: $x \in (-\infty, 1) \cup (1, \infty)$.

- Asymptotes:

Vertical: $x = 1$.

Horizontal: $y = 0$.

- There is no any point of inflection, maximum-minimum points.

- Function increasing on the interval: $x \in \emptyset$. Function decreasing on the interval:

$$x \in (-\infty, 1) \cup (1, \infty).$$

- Function concave up: $x \in (-\infty, 1)$. Function concave down: $x \in (1, \infty)$.

