

$$v = \frac{ds}{dt} \rightarrow ds = v dt$$

$$a = \frac{dv}{dt} \rightarrow dt = \frac{dv}{a}$$

$$ds = \frac{v dv}{a}$$

$$\int_0^S ds = \frac{1}{a} \int_{v_{initial}}^{v_{final}} v dv = \frac{1}{a} \frac{v^2}{2} \Big|_{v_{initial}}^{v_{final}} = \frac{1}{a} \frac{v_{final}^2 - v_{initial}^2}{2} = S \rightarrow v_{final}^2 - v_{initial}^2 = 2aS$$

$$v_{final}^2 = v_{initial}^2 + 2aS$$