

Clearly  $k[x] \subseteq Z(R)$ . Conversely, if  $f = \sum a_i x^i \in Z(R)$ , then  $fa = af$  for all  $a \in K$  shows that each  $a_i \in Z(K) = k$ , and hence  $f \in k[x]$ .