

Here A is the ring of all “skew polynomials” $\sum a_i x^i$ ($a_i \in \mathbb{C}$), multiplied according to the rule $xa = \sigma(a)x$ for $a \in \mathbb{C}$. Since $\sigma^2 = 1$, $x^2 a = \sigma^2(a)x^2 = ax^2$ for all $a \in \mathbb{C}$. This shows that $\mathbb{R}[x^2] \subseteq Z(A)$. Conversely, consider any $f = \sum a_r x^r \in Z(A)$. From $fa = af$, we have $a_r \sigma^r(a) = aa_r$ for all $a \in \mathbb{C}$. Setting $a = i$, we see that $a_r = 0$ for odd r . Therefore, $f = \sum a_{2s} x^{2s}$. From $fx = xf$, we see further that $\sigma(a_{2s}) = a_{2s}$, so $f \in \mathbb{R}[x^2]$.