

$$R = \{(a,b) | aRb\}$$

$$\forall (a,a): aRa$$

$$aRb \wedge bRc \Rightarrow aRc$$

$$R' = \{(a,b) | bRa\}$$

$$aR'b \equiv bRa$$

$$aRa \equiv aR'a$$

$$aR'b \wedge bR'c \Rightarrow bRa \wedge cRb \Rightarrow cRa \equiv aR'c$$

So,  $R'$  is again reflexive and transitive

Intersection of two reflexive and transitive relations is again reflexive and transitive relation.

If  $(a,b) \in R \cap R'$  then:

$$aRb \equiv bR'a \Rightarrow (b,a) \in R'$$

$$aR'b \equiv bRa \Rightarrow (b,a) \in R$$

$$(a,b) \in R \cap R' \Rightarrow (b,a) \in R \cap R'$$

Thus, intersection of reflexive and transitive relation and its inverse is **equivalence relation**.