

1) False:  $y = x^2$  has no fixed points on  $(0,1)$ , since  $x \neq x^2$  is always on this set.

2) True: The derivative of the function  $\log x$  is bounded on  $(0.5, +\infty)$ . So it is uniformly continuous

3) True: Given any sequence  $\{x_n + y_n\}$  on  $A+B$  we have:

$$x_n \xrightarrow{n \rightarrow \infty} x$$

$$y_n \xrightarrow{n \rightarrow \infty} y$$

$$|x_n + y_n - x - y| \leq |x_n - x| + |y_n - y| \xrightarrow{n \rightarrow \infty} 0$$

$$\lim(x_n + y_n) = x + y \in A + B$$

Thus, it is closed.

4) False: is quite easy to see that the function  $f(x) = \sin(x^2)$  for  $x$  in  $\mathbb{R}$  is bounded, continuous but not uniform continuous since  $[\sqrt{\pi/2 + (k+1)\pi} - \sqrt{\pi/2 + k\pi}] \rightarrow 0$  as  $k \rightarrow \infty$

5) True:  $f_n$  are continuous over closed interval, so they are uniformly bounded, and since they are all integrable, and their limit is too integrable, then we integral and limit sing commutes.