

$$\frac{z - \frac{1}{z}}{1 - \frac{1}{z}} = \frac{\frac{z^2 - 1}{z}}{\frac{z - 1}{z}} = \frac{(z + 1)(z - 1)}{z - 1} = z + 1$$