

A personnel manager has found that historically the scores on aptitude tests given to applicants for entry-level positions follow a normal distribution with a standard deviation of 32.4 points. A random sample of nine test scores from the current group of applicants had a mean score of 187.9 points.

- Find an 80% confidence interval for the population mean score of the current group of applicants.
- Based on these sample results, a statistician found for the population mean a confidence interval extending from 165.8 to 210.0 points. Find the confidence level of this interval.

$$n = 9$$

$$a = 187.9$$

$$d = 32.4$$

- Find an 80% confidence interval for the population mean score of the current group of applicants.

$$P(a - t < x < a + t) = 0.8$$

$$P(a - t < x < a + t) = P(-t < x - a < t) = P\left(\frac{-t}{d} < \frac{x - a}{d} < \frac{t}{d}\right) = \text{Central limit theorem} =$$

$$= F\left(\frac{t}{d}\right) - F\left(-\frac{t}{d}\right) = 2F\left(\frac{t}{d}\right) - 1 = 0.8$$

$$F\left(\frac{t}{d}\right) = 0.9$$

$$\frac{t}{d} = 1.28 - \text{this value is from table}$$

$$t = 1.28d = 41.472$$

interval is (187.9 - 41.472, 187.9 + 41.472)

- Based on these sample results, a statistician found for the population mean a confidence interval extending from 165.8 to 210.0 points. Find the confidence level of this interval.

$$P(165.8 < x < 210.0) = u - \text{confidence level}$$

$$P(-22.1 < x - 187.9 < 22.1) = u$$

$$P\left(\frac{-22.1}{d} < \frac{x - a}{d} < \frac{22.1}{d}\right) = \text{Central limit theorem} =$$

$$= F\left(\frac{22.1}{d}\right) - F\left(-\frac{22.1}{d}\right) = 2F\left(\frac{22.1}{32.4}\right) - 1 = u$$

$$2F(0.68) - 1 = 2 * 0.7517 - 1 = 0.5034$$

$$\text{confidence level} = 0.5$$