

Assume a binomial probability distribution with $n = 40$ and $\pi = .55$. Compute the following:

- The mean and standard deviation of the random variable.
- The probability that X is 25 or greater.
- The probability that X is 15 or less.
- The probability that X is between 15 and 25, inclusive.

$$E_x = \sum_{i=0}^{40} i * C_{40}^i p^i (1-p)^{40-i} =$$

$$\sum_{i=1}^{40} \frac{40! i 0.55^i (1-0.55)^{40-i}}{i! (40-i)!} = 22$$

$$D_x = \sum_{i=0}^{40} i^2 * C_{40}^i p^i (1-p)^{40-i} - 22^2 = 493.9 - 484 = 9.9$$

$$\text{standard deviation} = d = \sqrt{9.9} = 3.14$$

- The probability that X is 25 or greater.

$$P = \sum_{i=25}^{40} C_{40}^i p^i (1-p)^{40-i} = 0.214214$$

- The probability that X is 15 or less

$$P = \sum_{i=0}^{15} C_{40}^i p^i (1-p)^{40-i} = 0.0195775$$

- The probability that X is between 15 and 25, inclusive.

$$P = \sum_{i=15}^{25} C_{40}^i p^i (1-p)^{40-i} = 0.858791$$