

### Answer on Question #52448-Engineering-Other

A circuit consists of three blocks connected in series. The first block consists of a resistor of 31 ohm, and a capacitance of 100  $\mu\text{F}$  connected in parallel. The second block consists of a resistor of 50 ohm. The third block consists of a resistor of 20 ohm and an inductance of 0.11 H connected in parallel. The circuit is connected to a supply of 230 V at 50 Hz. Determine the overall current taken from the supply and its phase using the complex notations.

#### Solution

The overall current taken from the supply is

$$I = \frac{V}{Z}$$

The impedance is

$$Z = Z_1 + Z_2 + Z_3.$$

$$Z_1 = \frac{R_1 \left( \frac{1}{i\omega C_1} \right)}{R_1 + \frac{1}{i\omega C_1}} = \frac{R_1 \left( \frac{1}{i\omega C_1} \right) \left( R_1 - \frac{1}{i\omega C_1} \right)}{\left( R_1 + \frac{1}{i\omega C_1} \right) \left( R_1 - \frac{1}{i\omega C_1} \right)} = \frac{R_1 \left( \frac{1}{\omega C_1} \right) \left( \frac{1}{\omega C_1} - iR_1 \right)}{R_1^2 + \left( \frac{1}{\omega C_1} \right)^2}.$$

$$\frac{1}{\omega C_1} = \frac{1}{2\pi 50 \text{ Hz} \cdot 100 \mu\text{F}} = 32 \text{ ohm.}$$

$$Z_1 = \frac{31(32)(32 - i31)}{31^2 + (32)^2} = (16 - 15.5i) \text{ ohm.}$$

$$Z_2 = 50 \text{ ohm.}$$

$$Z_3 = \frac{R_3(i\omega L)}{R_3 + i\omega L} = \frac{R_3(i\omega L)(R_3 - i\omega L)}{(R_3 + i\omega L)(R_3 - i\omega L)} = \frac{R_3(\omega L)(iR_3 + \omega L)}{R_3^2 + (\omega L)^2}.$$

$$\omega L = 2\pi 50 \text{ Hz} \cdot 0.11 \text{ H} = 34.6 \text{ ohm.}$$

$$Z_3 = \frac{20(34.6)(i20 + 34.6)}{20^2 + 34.6^2} = (8.7i + 15) \text{ ohm.}$$

$$Z = 16 - 15.5i + 50 + 8.7i + 15 = (81 - 6.8i) \text{ ohm.}$$

$$I = \frac{230 \angle 0^\circ}{(81 - 6.8i)} = 2.8A \angle 4.8^\circ.$$

**Answer:  $2.8A \angle 4.8^\circ$ .**