Answer on Question #47363, Engineering, Other

One sample has n = 4 scores and M = 10. A second sample has n = 6 scores and M = 5. If the two samples are combined, then what is the mean for the combined sample?

Solution:

In our task we have the following data: $Mean_1 = 10$, $n_1 = 4$ scores, $Mean_2 = 5$, $n_1 = 6$ scores.

The mean (more precisely, the arithmetic mean) is commonly called the average. It is the sum of the data, divided by the number of data:

Mean =
$$\frac{\text{sum of data}}{\text{number of data}} = \frac{\text{total}}{\text{number of data}} = \frac{1}{n} \sum_{k=1}^{n} x_k$$

We start to find sum of the first sample. From the formula noted above we can find total sum.

Sum of data = Mean₁
$$\cdot$$
 n₁ = 10 \cdot 4 = 40

Then we find the sum for the second sample of data. Substitute the given values.

Sum of data =
$$Mean_2 \cdot n_2 = 5 \cdot 6 = 30$$

Now we can find the new score for combined data, which will be equal:

$$n = n_1 + n_2 = 4 + 6 = 10$$
 scores

Also we can find the new sum of combined data, which will be equal:

Sum of data = Mean₁
$$\cdot$$
 n₁ + Mean₂ \cdot n₂ = 40 + 30 = 70

Finally we can find the new Mean of the combined data. We substitute the values of sum data and total scores.

$$Mean = \frac{Mean_1 \cdot n_1 + Mean_2 \cdot n_2}{n_1 + n_2} = \frac{70}{10} = 7$$
$$Mean = 7$$

Accordingly we found the value of new Mean, which is equal to 7.