

Answer on Question #45204, Engineering, Other

Task: 1) Show that $\cos A \cdot \cos B = 0.5(\cos(A + B) + \cos(A - B))$. Some English is essential in addition to the algebra. Note that cosine is an even function so that $\cos(A - B) = \cos(B - A)$.
2) A mixer has a local oscillator at 1157 kHz and a bandpass filter centered at 455 kHz. What are the center frequencies of signals which would cause output from the filter? How is it that a radio receiver accepts only one channel of input signal?

Solution:

1)

$$\begin{aligned}\cos(A + B) &= \cos A \cos B - \sin A \sin B \\ \cos(A - B) &= \cos A \cos B + \sin A \sin B \Rightarrow \\ 0.5(\cos(A + B) + \cos(A - B)) &= \cos A \cos B - \sin A \sin B + \cos A \cos B + \sin A \sin B = \\ &= 0.5 \cdot 2 \cos A \cos B = \cos A \cos B \Rightarrow \\ \cos A \cos B &= \cos A \cos B\end{aligned}$$

So, we show that $\cos A \cdot \cos B = 0.5(\cos(A + B) + \cos(A - B))$

2) What are the center frequencies of signals which would cause output from the filter?

$$\text{Answer: } f_{cf} = f_l - f_c = 1157 - 455 = 702 \text{ kHz}$$