

Answer on Question #39434 – Economics – Microeconomics

The demand for good X is given by this equation:

$$Q_X = 1.0 - 2.0P_X + 0.8I + 1.5P_Y - 3P_Z + 1.0A,$$

where P_X , P_Y , and P_Z represent the prices of goods X, Y, and Z; I measures income per capita; and A is advertising.

$$P_X = 2.00, P_Y = 2.50, P_Z = 1.00, I = 4, \text{ and } A = 3.05.$$

A. Is good X a necessity or a luxury good? How do you know?

$$Q_X = 1 - 2*2 + 0.8*4 + 1.5*2.5 - 3*1 + 1*3.05 = 4 \text{ units}$$

It is a luxury good, as its quantity is only 4 units.

B. Calculate the cross elasticity of demand for X with respect to the price of good Z. Are goods X and Z substitutes or complements?

$$E_{A,B} = \frac{P_{B,1} + P_{B,2}}{Q_{A,1} + Q_{A,2}} \times \frac{\Delta Q_A}{\Delta P_B} = \frac{\partial Q_A}{\partial P_B} \frac{P_B}{Q_A}$$

So, $E_{X,Z} = k * P_Z / Q_X = -2 * 1 / 4 = -0.5$, where k is coefficient before P_X as the derivative of $\Delta Q / \Delta P$.

Two goods that complement each other show a negative cross elasticity of demand: as the price of good Y rises, the demand for good X falls. So, x and z are complements.

C. Calculate the advertising elasticity of demand for X. Interpret your answer.

$$E_d = \frac{P}{Q_d} \times \frac{dQ_d}{dP}$$

So, $E_d = k * A / Q_X = -2 * 3.05 / 4 = -1.525$, where k is coefficient before P_X as the derivative of $\Delta Q / \Delta P$, so the advertising is elastic as $E_d < -1$.

D. What kind of change in the price of X would you recommend if the firm is interested in maximizing revenue?

As the advertising is elastic, the decrease in price will increase the revenue, as the change in quantity demanded will be higher than the change in price.