

Answer on Question #81410, Chemistry/ Organic Chemistry

Calculate the total amount of heat energy in kilocalories that must be released in order to condense 18.9 g of steam at 373.0 K, cool that liquid to 272.0 K, then freeze the liquid at 272.0 K.

Solution

latent heat of fusion of ice = 335 J/g,

latent heat of vaporisation of water = 2260 J/g,

specific heat capacity of ice = 2.14 J/(g °C),

specific heat capacity of water = 4.184 J/(g °C)

specific heat capacity of steam = 2.01 J/(g °C).

The energy released is determined in 4 stages:

$$Q = Q_1 + Q_2 + Q_3 + Q_4$$

1. Find Q_1 – the heat of phase change (steam-water) at 373.0 K (or $T(^{\circ}\text{C}) = 373 - 273 = 100^{\circ}\text{C}$):

$$Q_1 = L_v \times m, \text{ where } L_v = 2260 \text{ J/g},$$

$$Q_1 = 2260 \text{ J/g} \times 18.9 \text{ g} = 2.23 \cdot 10^6 \text{ J} = 42714 \text{ J}.$$

As Q is released then $Q_1 = -42714 \text{ J}$

2. Find Q_2 – heat that is released when the temperature of water changes from 373 K to 273 K (or from 100°C to 0°C)

$$Q_2 = cm(T_2 - T_1), \text{ where } c \text{ (for water)} = 4.184 \text{ J/g}\cdot^{\circ}\text{C}$$

$$Q_2 = 4.184 \text{ J/g}\cdot^{\circ}\text{C} \cdot 18.9 \text{ g} \cdot (0 - 100)^{\circ}\text{C} = -7907.8 \text{ J}$$

3. Find Q_3 – the heat of phase change (water-ice):

$$Q_3 = L_f \times m, \text{ where } L_f = 335 \text{ J/g}$$

$$Q_3 = 335 \text{ J/g} \cdot 18.9 \text{ g} = 6331.5 \text{ J}$$

As Q is released then $Q_3 = -6331.5 \text{ J}$

4. Find Q_4 – heat that is released when the temperature changes from 273 K to 272 K (or from 0°C to -1°C).

$$Q_4 = cm(T_2 - T_1), \text{ where } c \text{ (for ice)} = 2.14 \text{ J/g}\cdot^{\circ}\text{C}$$

$$Q_4 = 2.14 \text{ J/g}\cdot^{\circ}\text{C} \cdot 18.9 \text{ g} \cdot (-1 - 0)^{\circ}\text{C} = -40.4 \text{ J}$$

$$Q = Q_1 + Q_2 + Q_3 + Q_4 = -42714 \text{ J} - 7907.8 \text{ J} - 6331.5 \text{ J} - 40.4 \text{ J} = -56993.7 \text{ J}$$

The sign “-” shows that the system loses 56993.7 J of energy releasing this amount of energy into surrounding. So, surrounding gets is 56993.7 J of energy or $56993.7 \text{ J} \times 0.2388 \text{ cal/J} = 13610 \text{ cal} = 13.6 \text{ kcal}$.

Answer: 13.6 kcal