

Answer on Question #75754, Chemistry / Inorganic Chemistry

Using Bohr atomic model derive expression for calculating orbits in He⁺ using this expression calculate the radius of fourth orbital of he⁺ion

Solution

1. Expression for calculating orbits in He⁺.

Coulomb force is centripetal when electron moves in orbit. Then

$$\frac{Ze \cdot e}{4\pi\epsilon_0 r^2} = \frac{mv^2}{r};$$

$$r = \frac{Ze^2}{4\pi\epsilon_0 mv^2}.$$

According to Bohr postulates the angular momentum of stationary electron is quantized:

$$mvr = nh/2\pi; \Rightarrow v = nh/2\pi mr.$$

Then

$$r = \frac{Ze^2}{4\pi\epsilon_0 mv^2} = \frac{Ze^2 4\pi^2 m^2 r^2}{4\pi\epsilon_0 mn^2 h^2} = \frac{Ze^2 \pi m r^2}{\epsilon_0 n^2 h^2} \Rightarrow r = \frac{\epsilon_0 h^2}{Ze^2 \pi m} \cdot n^2, \text{ where } n = 1, 2, 3, \dots$$

Z(He⁺) = 2, then

$$r = \frac{\epsilon_0 h^2}{2e^2 \pi m} \cdot n^2, \text{ where } n = 1, 2, 3, \dots$$

2. The radius of fourth orbital of He⁺ ion

$$r_4 = \frac{\epsilon_0 h^2}{Ze^2 \pi m} \cdot n^2 = \frac{8.85 \cdot 10^{-12} \cdot (6.626 \cdot 10^{-34})^2}{2 \cdot (1.6 \cdot 10^{-19})^2 \cdot 3.14 \cdot 9.1 \cdot 10^{-31}} \cdot 4^2 = 4.25 \cdot 10^{-10} \text{ (m)}.$$

Answer: 1.
$$r = \frac{\epsilon_0 h^2}{2e^2 \pi m} \cdot n^2, \text{ where } n = 1, 2, 3, \dots$$

2. $r_4 = 4.25 \cdot 10^{-10} \text{ m}$